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elseif(($l1 == 0 and $m1 == 0 and $l2 == 2 and $m2 == -2) or
        ($l1 == 2 and $m1 == -2 and $l2 == 0 and $m2 == 0)) { #sxy
    $b = sqrt(3.0)*$lx*$ly * $VS; OK
}
elseif(($l1 == 0 and $m1 == 0 and $l2 == 2 and $m2 == -1) or
        ($l1 == 2 and $m1 == -1 and $l2 == 0 and $m2 == 0)) { #syz
    $b = sqrt(3.0)*$ly*$lz * $VS; OK
}
elseif(($l1 == 0 and $m1 == 0 and $l2 == 2 and $m2 == 0) or
        ($l1 == 2 and $m1 == 0 and $l2 == 0 and $m2 == 0)) { #s3z2-r2
    $b = ($lz2 - 0.5*($lx2 + $ly2)) * $VS; OK
}
elseif(($l1 == 0 and $m1 == 0 and $l2 == 2 and $m2 == 1) or
        ($l1 == 2 and $m1 == 1 and $l2 == 0 and $m2 == 0)) { #szx
    $b = sqrt(3.0)*$lz*$lx * $VS; OK
}
elseif(($l1 == 0 and $m1 == 0 and $l2 == 2 and $m2 == 2) or
        ($l1 == 2 and $m1 == 2 and $l2 == 0 and $m2 == 0)) { #sx2-y2
    $b = 0.5 * sqrt(3.0) * ($lx2 - $ly2) * $VS; OK
}
elseif(($l1 == 1 and $m1 == -1 and $l2 == 2 and $m2 == -2)) { #y xy
    $b = $lx*$ly*$lz*(sqrt(3.0) * $VS - 2.0*$VP);
}
elseif(($l1 == 2 and $m1 == -2 and $l2 == 1 and $m2 == -1)) { #xy y
    $b = $lx*$ly*$lz*(sqrt(3.0) * $VS - 2.0*$VP);
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == -1 and $l2 == 2 and $m2 == -1)) { #y yz
    $b = sqrt(3.0) * $ly2*$lz * $VS + $lz*(1.0-2.0*$ly2) * $VP; OK
}
elseif(($l1 == 2 and $m1 == -1 and $l2 == 1 and $m2 == -1)) { #yz y
    $b = sqrt(3.0) * $ly2*$lz * $VS + $lz*(1.0-2.0*$ly2) * $VP; OK
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == -1 and $l2 == 2 and $m2 == 0)) { #y 3z2-r2
    $b = $ly*($lz2-0.5*($lx2+$ly2)) * $VS - sqrt(3.0) * $ly*($lx2+$y2) * $
    VP;
}
elseif(($l1 == 2 and $m1 == 0 and $l2 == 1 and $m2 == -1)) { #3z2-r2 y
    $b = $ly*($lz2-0.5*($lx2+$ly2)) * $VS - sqrt(3.0) * $ly*($lx2+$y2) * $
    VP;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == -1 and $l2 == 2 and $m2 == 1)) { #y zx
    $b = $lx*$ly*$lz * (sqrt(3.0) * $VS - 2.0 * $VP); OK
}
elseif(($l1 == 2 and $m1 == 1 and $l2 == 1 and $m2 == -1)) { #zx y
    $b = $lx*$ly*$lz * (sqrt(3.0) * $VS - 2.0 * $VP);
    $b = -$b; OK
}
elseif(($l1 == 1 and $m1 == -1 and $l2 == 2 and $m2 == 2)) { #y x2-y2

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    $b = 0.5*sqrt(3.0) * $ly*($lx2-$ly2) * $VS - $ly*(1.0+$lx2-$ly2) * $V
    P;
}
elseif(($l1 == 2 and $m1 == 2 and $l2 == 1 and $m2 == -1)) { #x2-y2 y
    $b = 0.5*sqrt(3.0) * $ly*($lx2-$ly2) * $VS - $ly*(1.0+$lx2-$ly2) * $V
    P;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 0 and $l2 == 2 and $m2 == -2)) { #x xy
    $b = $lx*$ly*$lz * (sqrt(3.0) * $VS - 2.0 * $VP);
}
elseif(($l1 == 2 and $m1 == -2 and $l2 == 1 and $m2 == 0)) { #xy z
    $b = $lx*$ly*$lz * (sqrt(3.0) * $VS - 2.0 * $VP);
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 0 and $l2 == 2 and $m2 == -1)) { #z yz
    $b = sqrt(3.0) * $lz2*$ly * $VS + $ly*(1.0-2.0*$lz2) * $VP;
}
elseif(($l1 == 2 and $m1 == -1 and $l2 == 1 and $m2 == 0)) { #yz z
    $b = sqrt(3.0) * $lz2*$ly * $VS + $ly*(1.0-2.0*$lz2) * $VP;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 0 and $l2 == 2 and $m2 == 0)) { #z 3z2-r2
    $b = $lz*($lz2-0.5*($lx2+$ly2)) * $VS + sqrt(3.0)*$lz*($lx2+$ly2) * $V
    P;
}
elseif(($l1 == 2 and $m1 == 0 and $l2 == 1 and $m2 == 0)) { #3z2-r2 z
    $b = $lz*($lz2-0.5*($lx2+$ly2)) * $VS + sqrt(3.0)*$lz*($lx2+$ly2) * $V
    P;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 0 and $l2 == 2 and $m2 == 1)) { #z zx
    $b = sqrt(3.0)*$lz2*$lx * $VS + $lx*(1.0-2.0*$lz) * $VP;
}
elseif(($l1 == 2 and $m1 == 0 and $l2 == 1 and $m2 == 0)) { #zx z
    $b = sqrt(3.0)*$lz2*$lx * $VS + $lx*(1.0-2.0*$lz) * $VP;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 0 and $l2 == 2 and $m2 == 2)) { #z x2-y2
    $b = 0.5*sqrt(3.0)*$lz*($lx2-$ly2) * $VS - $lz*($lx2-$ly2) * $VP;
}
elseif(($l1 == 2 and $m1 == 2 and $l2 == 1 and $m2 == 0)) { #x2-y2 z
    $b = 0.5*sqrt(3.0)*$lz*($lx2-$ly2) * $VS - $lz*($lx2-$ly2) * $VP;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 1 and $l2 == 2 and $m2 == -2)) { #x xy
    $b = sqrt(3.0) * $lx2*$ly * $VS + $ly*(1.0-2.0*$lx2) * $VP;
}
elseif(($l1 == 2 and $m1 == -2 and $l2 == 1 and $m2 == 1)) { #xy x
    $b = sqrt(3.0) * $lx2*$ly * $VS + $ly*(1.0-2.0*$lx2) * $VP;
    $b = -$b;
}

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}
elseif(($l1 == 1 and $m1 == 1 and $l2 == 2 and $m2 == -1)) { #x yz
    $b = $lx*$ly*$lz * (sqrt(3.0) * $VS - 2.0*$VP);
}
elseif(($l1 == 2 and $m1 == -1 and $l2 == 1 and $m2 == 1)) { #yz x
    $b = $lx*$ly*$lz * (sqrt(3.0) * $VS - 2.0*$VP);
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 1 and $l2 == 2 and $m2 == 0)) { #x 3z2-r2
$b = $lx*($lz2-0.5*($lx2+$ly2)) * $VS - sqrt(3.0) * $lx*$lz2 * $VP;
elseif(($l1 == 2 and $m1 == 0 and $l2 == 1 and $m2 == 1)) { #3z2-r2 x
$b = $lx*($lz2-0.5*($lx2+$ly2)) * $VS - sqrt(3.0) * $lx*$lz2 * $VP;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 1 and $l2 == 2 and $m2 == 1)) { #x zx
    $b = sqrt(3.0)*$lx2*$lz * $VS + $lz*(1.0-2.0*$lx2) * $VP;
}
elseif(($l1 == 2 and $m1 == 1 and $l2 == 1 and $m2 == 1)) { #zx x
    $b = sqrt(3.0)*$lx2*$lz * $VS + $lz*(1.0-2.0*$lx2) * $VP;
    $b = -$b;
}
elseif(($l1 == 1 and $m1 == 1 and $l2 == 2 and $m2 == 2)) { #x x2-y2
    $b = 0.5*sqrt(3.0)*$lx*($lx2-$ly2) * $VS + $lx*(1.0-$lx2+$ly2) * $VP;
}
elseif(($l1 == 2 and $m1 == 2 and $l2 == 1 and $m2 == 1)) { #x x2-y2
    $b = 0.5*sqrt(3.0)*$lx*($lx2-$ly2) * $VS + $lx*(1.0-$lx2+$ly2) * $VP;
    $b = -$b;
}

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$$\begin{aligned}
 E_{s, x^2 - y^2} &= \frac{1}{2} 3^{1/2} (l^2 - m^2) V_{sd\sigma} && \begin{matrix} l & m & n \\ x & y & z \end{matrix} \\
 E_{s, 3z^2 - r^2} &= [n^2 - \frac{1}{2}(l^2 + m^2)] V_{sd\sigma} \\
 E_{x, xy} &= 3^{1/2} l^2 m V_{pd\sigma} + m(1 - 2l^2) V_{pd\pi} \\
 E_{x, yz} &= 3^{1/2} l m n V_{pd\sigma} - 2 l m n V_{pd\pi} \\
 E_{x, zx} &= 3^{1/2} l^2 n V_{pd\sigma} + n(1 - 2l^2) V_{pd\pi} \\
 E_{x, x^2 - y^2} &= \frac{1}{2} 3^{1/2} l (l^2 - m^2) V_{pd\sigma} + l(1 - l^2 + m^2) V_{pd\pi} \\
 E_{y, x^2 - y^2} &= \frac{1}{2} 3^{1/2} m (l^2 - m^2) V_{pd\sigma} - m(1 + l^2 - m^2) V_{pd\pi} \\
 E_{z, x^2 - y^2} &= \frac{1}{2} 3^{1/2} n (l^2 - m^2) V_{pd\sigma} - n(l^2 - m^2) V_{pd\pi} \\
 E_{x, 3z^2 - r^2} &= l [n^2 - \frac{1}{2}(l^2 + m^2)] V_{pd\sigma} - 3^{1/2} l n^2 V_{pd\pi} \\
 E_{y, 3z^2 - r^2} &= m [n^2 - \frac{1}{2}(l^2 + m^2)] V_{pd\sigma} - 3^{1/2} m n^2 V_{pd\pi} \\
 E_{z, 3z^2 - r^2} &= n [n^2 - \frac{1}{2}(l^2 + m^2)] V_{pd\sigma} + 3^{1/2} n (l^2 + m^2) V_{pd\pi} \\
 E_{xy, xy} &= 3l^2 m^2 V_{dd\sigma} + (l^2 + m^2 - 4l^2 m^2) V_{dd\pi} + (n^2 + l^2 m^2) V_{dd\delta} \\
 E_{xy, yz} &= 3l m^2 n V_{dd\sigma} + l n (1 - 4m^2) V_{dd\pi} + l n (m^2 - 1) V_{dd\delta} \\
 E_{xy, zx} &= 3l^2 m n V_{dd\sigma} + m n (1 - 4l^2) V_{dd\pi} + m n (l^2 - 1) V_{dd\delta} \\
 E_{xy, x^2 - y^2} &= \frac{3}{2} l m (l^2 - m^2) V_{dd\sigma} + 2 l m (m^2 - l^2) V_{dd\pi} + \frac{1}{2} l m (l^2 - m^2) V_{dd\delta}
 \end{aligned}$$

$$\begin{aligned}
E_{y, 3z^2-r^2} &= m[n^2 - \frac{1}{2}(l^2 + m^2)]V_{pds} - 3^{1/2}mn^2V_{pdn} \\
E_{z, 3z^2-r^2} &= n[n^2 - \frac{1}{2}(l^2 + m^2)]V_{pds} + 3^{1/2}n(l^2 + m^2)V_{pdn} \\
E_{xy, xy} &= 3l^2m^2V_{dds} + (l^2 + m^2 - 4l^2m^2)V_{ddn} + (n^2 + l^2m^2)V_{ddb} \\
E_{xy, yz} &= 3lm^2nV_{dds} + ln(1 - 4m^2)V_{ddn} + ln(m^2 - 1)V_{ddb} \\
E_{xy, zx} &= 3l^2mnV_{dds} + mn(1 - 4l^2)V_{ddn} + mn(l^2 - 1)V_{ddb} \\
E_{xy, x^2-y^2} &= \frac{3}{2}lm(l^2 - m^2)V_{dds} + 2lm(m^2 - l^2)V_{ddn} + \frac{1}{2}lm(l^2 - m^2)V_{ddb} \\
E_{yz, x^2-y^2} &= \frac{3}{2}mn(l^2 - m^2)V_{dds} - mn[1 + 2(l^2 - m^2)]V_{ddn} + mn[1 + \frac{1}{2}(l^2 - m^2)]V_{ddb} \\
E_{zx, x^2-y^2} &= \frac{3}{2}nl(l^2 - m^2)V_{dds} + nl[1 - 2(l^2 - m^2)]V_{ddn} - nl[1 - \frac{1}{2}(l^2 - m^2)]V_{ddb} \\
E_{xy, 3z^2-r^2} &= 3^{1/2}lm[n^2 - \frac{1}{2}(l^2 + m^2)]V_{dds} - 3^{1/2}2lmn^2V_{ddn} + \frac{1}{2}3^{1/2}lm(1 + n^2)V_{ddb} \\
E_{yz, 3z^2-r^2} &= 3^{1/2}mn[n^2 - \frac{1}{2}(l^2 + m^2)]V_{dds} + 3^{1/2}mn(l^2 + m^2 - n^2)V_{ddn} - \frac{1}{2}3^{1/2}mn(l^2 + m^2)V_{ddb} \\
E_{zx, 3z^2-r^2} &= 3^{1/2}ln[n^2 - \frac{1}{2}(l^2 + m^2)]V_{dds} + 3^{1/2}ln(l^2 + m^2 - n^2)V_{ddn} - \frac{1}{2}3^{1/2}ln(l^2 + m^2)V_{ddb} \\
E_{x^2-y^2, x^2-y^2} &= \frac{3}{4}(l^2 - m^2)^2V_{dds} + [l^2 + m^2 - (l^2 - m^2)^2]V_{ddn} + [n^2 + \frac{1}{4}(l^2 - m^2)^2]V_{ddb} \\
E_{x^2-y^2, 3z^2-r^2} &= \frac{1}{2}3^{1/2}(l^2 - m^2)[n^2 - \frac{1}{2}(l^2 + m^2)]V_{dds} + 3^{1/2}n^2(m^2 - l^2)V_{ddn} \\
&\quad + \frac{1}{4}3^{1/2}(1 + n^2)(l^2 - m^2)V_{ddb} \\
E_{3z^2-r^2, 3z^2-r^2} &= [n^2 - \frac{1}{2}(l^2 + m^2)]^2V_{dds} + 3n^2(l^2 + m^2)V_{ddn} + \frac{3}{4}(l^2 + m^2)^2V_{ddb}
\end{aligned}$$
