

# Fermi-Surface Script Tutorial

Materials Theory and Design Group

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**MATERIALS  
THEORY AND  
DESIGN GROUP**

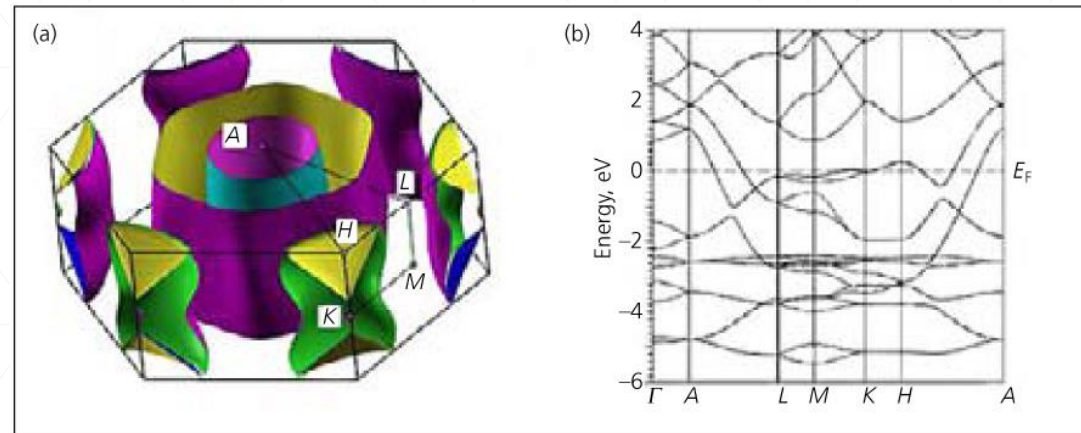
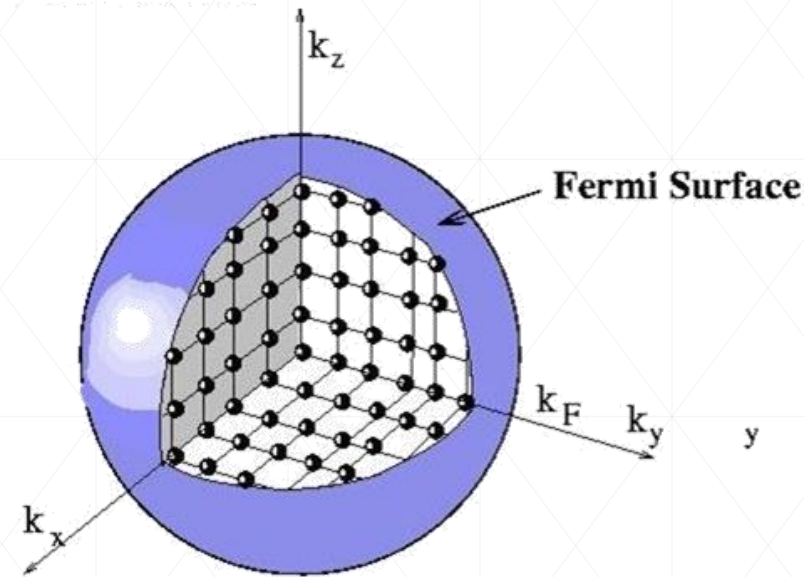


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# CONTENTS

- What is fermi surface
- How to draw fermi surface
- Fermi surface with VASP and Xcrysden: Python script

# Fermi Surface



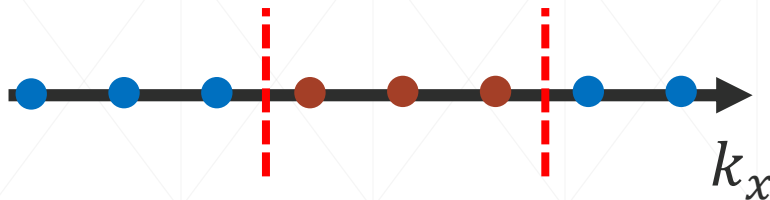
A. Ivanovskii, Platinum Metals Rev., 2013, 57, (2), 87

## Fermi Surface

- Abstract boundary in reciprocal space
- Useful for predicting the thermal, electrical, magnetic, and optical properties
- Derived from periodicity and symmetry of the crystalline lattice
- Direct consequence of Pauli exclusion principle, and occupation of electronic bands
- Visually more intuitive than providing band structure in some cases (e.g., 2DEG)

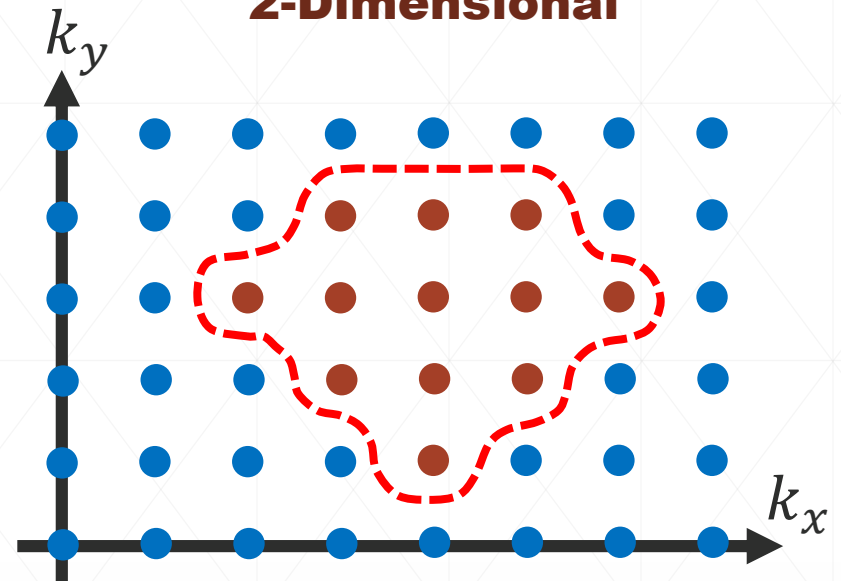
# Drawing Fermi Surface in 1-D and 2-D Cases

## 1-Dimensional



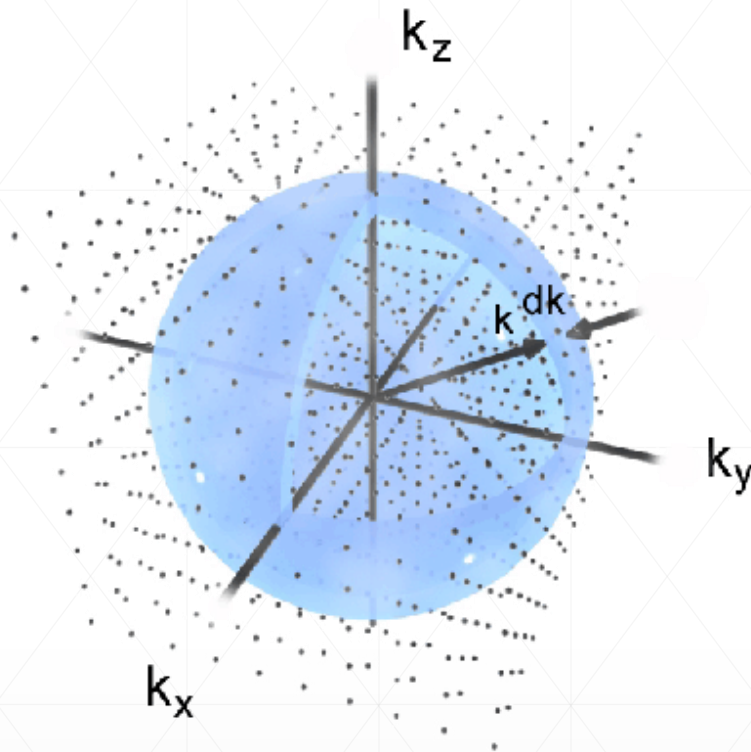
- Energy slightly over  $E_F$
- Energy slightly below  $E_F$

## 2-Dimensional

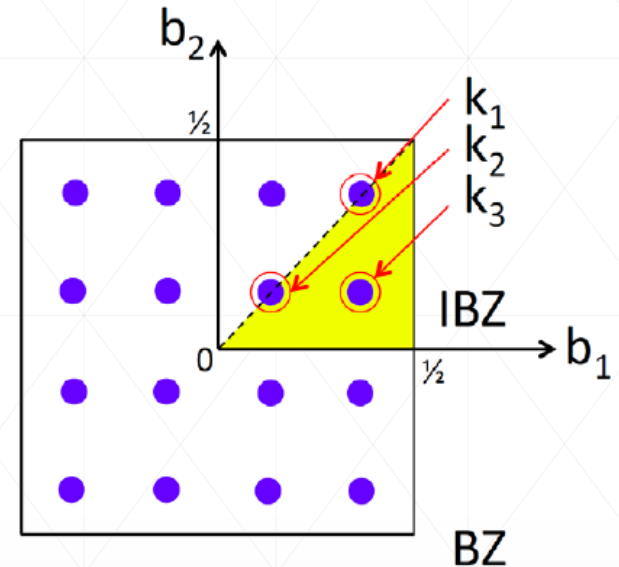


- Fermi surface is drawn where eigen energy of electronic band is equal to  $E_F$
- Multiple boundary can be given depending on electronic bands
- Total fermi surface is collection of the boundaries of all bands

# Drawing Fermi Surface in 3-D with VASP



## When $ISYM \neq -1$



- To draw fermi surface using VASP, 3-dimensional mesh grid should be prepared
- INCAR is very similar to band structure calculation, except for  $ISYM$  -tag
- $ISYM = -1$  # This is to turn off symmetry, and has easier data for do post-process
- Otherwise only Irreducible Brillouin Zone will be calculated on VASP

# Step 1: Prepare k-mesh grid

## Python script 'Fermi\_kpoints.py'

- How to use:  
\$ python Fermi\_kpoints.py KX KY KZ  
KX, KY, KZ (Optional): number of points along each reciprocal axis  
If not given, default value of 9 is assigned, which is quite high for usual structures.
- Output filename: 'KPOINTS'

## Output example

```
1 k-points for fermi-surface. RP-phase 9x9x9
2 729
3 Reciprocal
4 0.0000 0.0000 0.0000 1
5 0.0000 0.0000 0.1111 1
6 0.0000 0.0000 0.2222 1
7 0.0000 0.0000 0.3333 1
8 0.0000 0.0000 0.4444 1
9 0.0000 0.0000 0.5556 1
10 0.0000 0.0000 0.6667 1
11 0.0000 0.0000 0.7778 1
12 0.0000 0.0000 0.8889 1
13 0.0000 0.1111 0.0000 1
14 0.0000 0.1111 0.1111 1
15 0.0000 0.1111 0.2222 1
```

**Weight**

- Line 1: Comment
- Line 2: Total number of k-points
- Line 3: Reciprocal
- Line 4-end: reciprocal coordinate of each k-point and its **weight**.

# Step 2 & 3: VASP Calculation and Post-processing

## Step 2: VASP Calculation

- After self-consistent calculation, use CHGCAR for non self-consistent calculation
- INCAR: ISYM = -1, ICHARG = 11, ISMEAR = 0
- Required files for fermi surface: OUTCAR and EIGENVAL
- OUTCAR: information on reciprocal lattice and fermi energy ( $E_F$ )  
EIGENVAL: eigen energy values of electronic bands

## Step 3: Create .bxsf file (Script ' Fermi\_surface.py ')

- How to use:  
\$ python Fermi\_surface.py [OUTCAR\_file] [EIGENVAL\_file] [output.bxsf]  
[OUTCAR\_file] (optional): OUTCAR filename from calculation  
default: 'OUTCAR'  
[EIGENVAL\_file] (optional): EIGENVAL filename from calculation  
default: 'EIGENVAL'
- Output filename: [output.bxsf] (optional)  
default: 'Xcrysden.bxsf'
- Example: \$ python Fermi\_surface.py OUTCAR\_fermi EIGENVAL\_fermi Xcrysden.bxsf

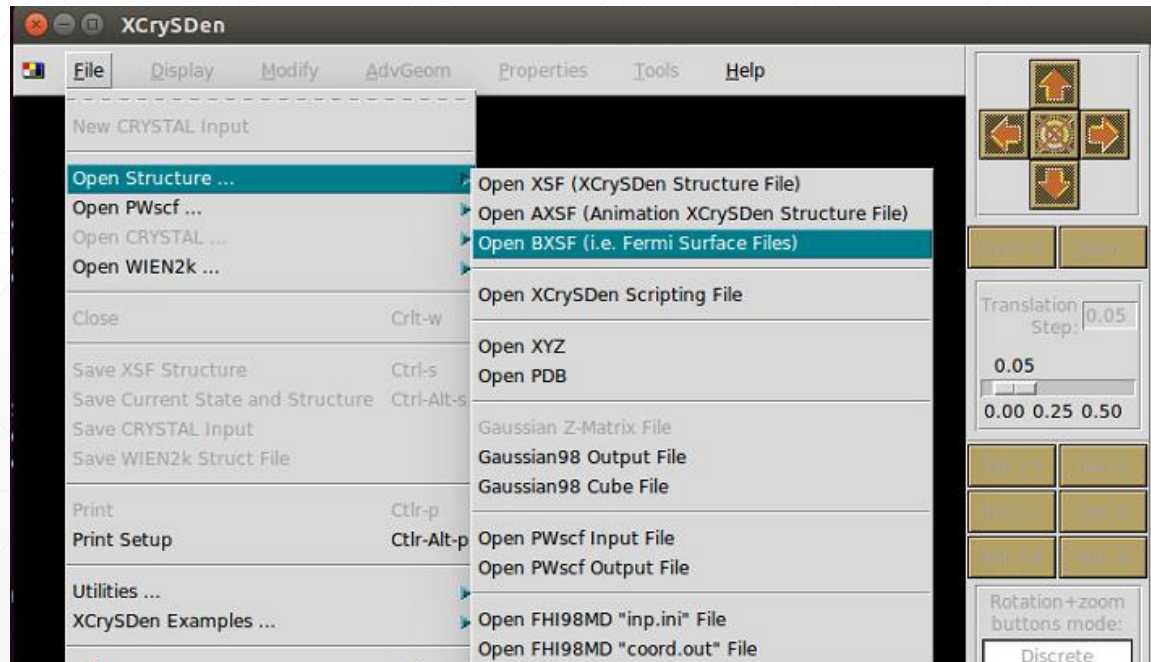


# Step 4: Run Xcrysden

## Xcrysden

- How to install: <http://www.xcrysden.org/Download.html>
- Input file: .bxsf file  
Information is given here, [http://www.xcrysden.org/doc/XSF.html#\\_\\_toc\\_\\_14](http://www.xcrysden.org/doc/XSF.html#__toc__14)
- Generated bxsf file is ready to use

## Step by step instruction

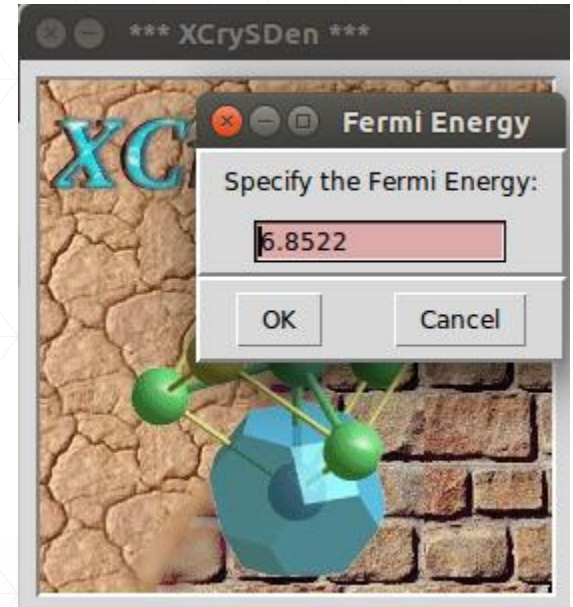
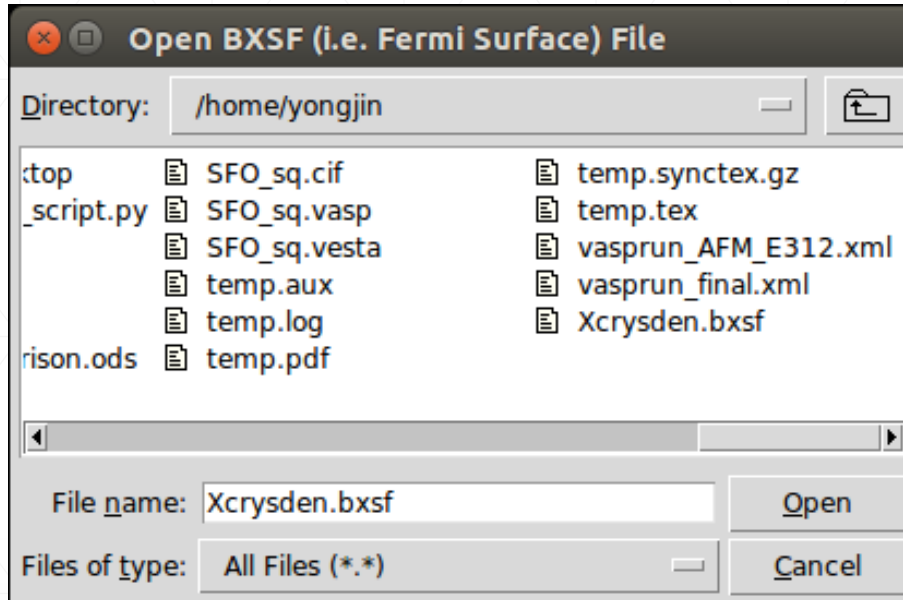


- File
  - Open Structure...
  - Open BXSf



# Step 4: Run Xcrysden

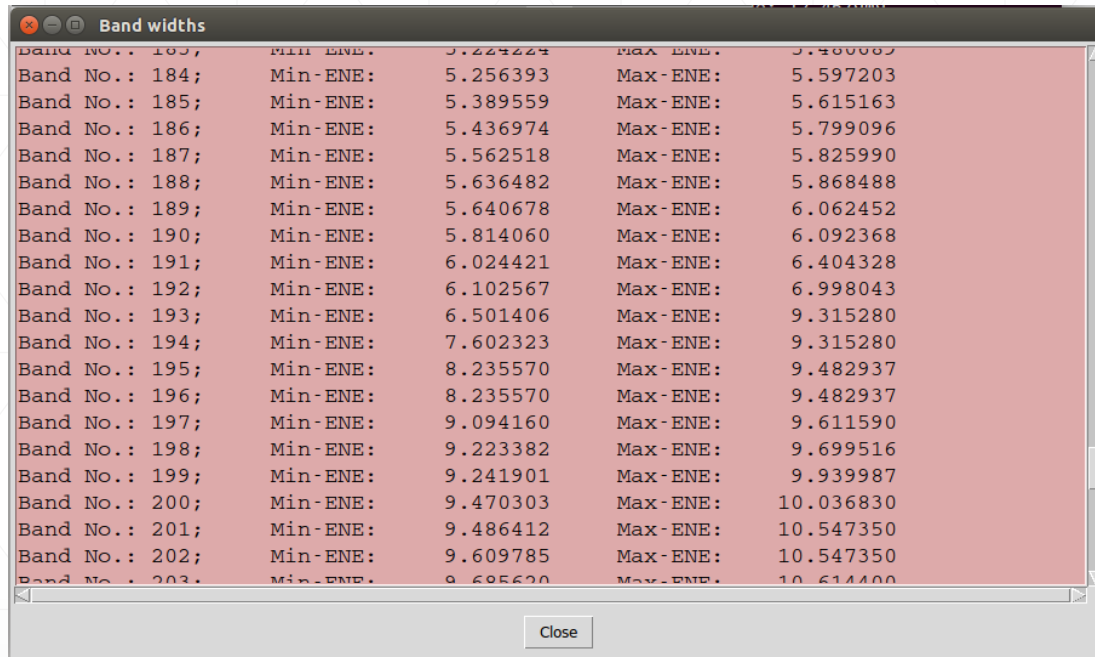
## Open file



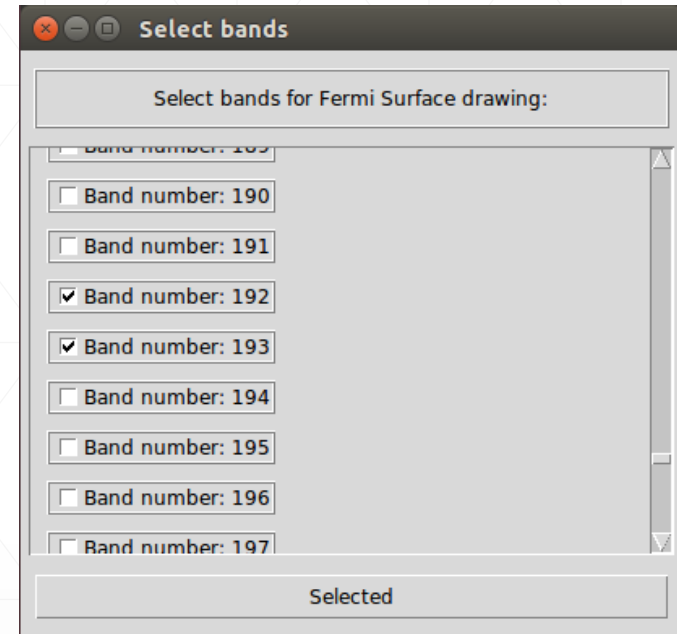
- Fermi energy is automatically filled in.
- Remember the value

# Step 4: Run Xcrysden

## Select Bands



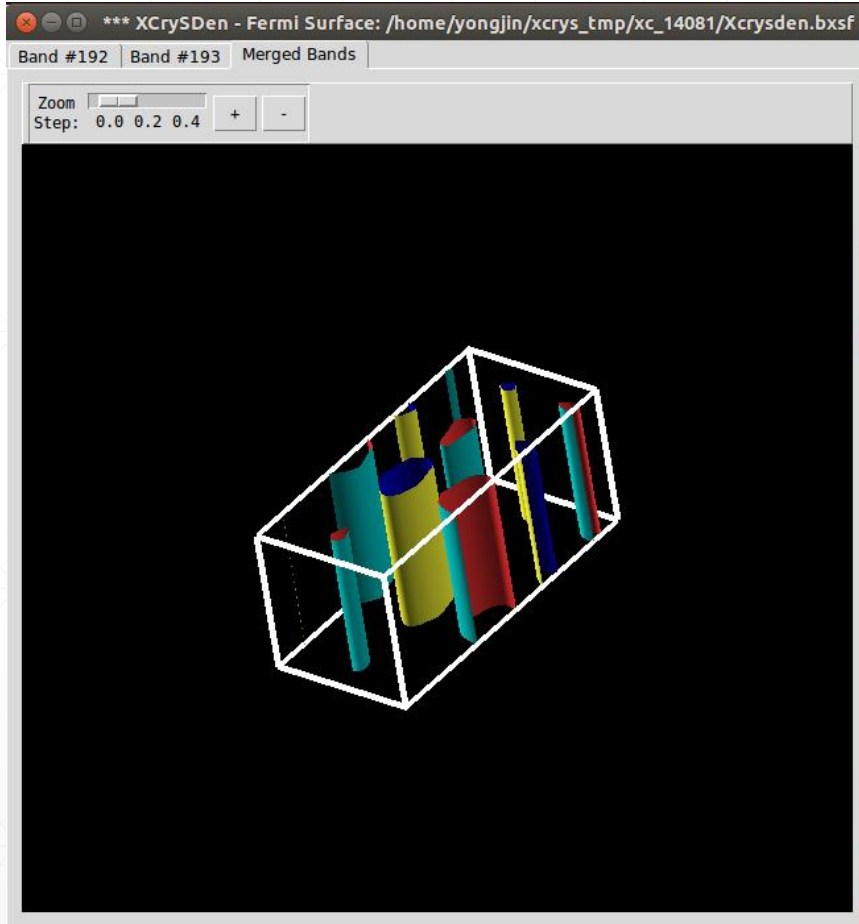
| Band No.: | Min-ENE: | Max-ENE:  |
|-----------|----------|-----------|
| 183;      | 5.224224 | 5.480003  |
| 184;      | 5.256393 | 5.597203  |
| 185;      | 5.389559 | 5.615163  |
| 186;      | 5.436974 | 5.799096  |
| 187;      | 5.562518 | 5.825990  |
| 188;      | 5.636482 | 5.868488  |
| 189;      | 5.640678 | 6.062452  |
| 190;      | 5.814060 | 6.092368  |
| 191;      | 6.024421 | 6.404328  |
| 192;      | 6.102567 | 6.998043  |
| 193;      | 6.501406 | 9.315280  |
| 194;      | 7.602323 | 9.315280  |
| 195;      | 8.235570 | 9.482937  |
| 196;      | 8.235570 | 9.482937  |
| 197;      | 9.094160 | 9.611590  |
| 198;      | 9.223382 | 9.699516  |
| 199;      | 9.241901 | 9.939987  |
| 200;      | 9.470303 | 10.036830 |
| 201;      | 9.486412 | 10.547350 |
| 202;      | 9.609785 | 10.547350 |
| 203;      | 9.685620 | 10.614400 |



- Find bands goes over  $E_F$ , and check on the other window
- You can check based on Min-ENE and Max-ENE of each band
- Bands are listed with increasing order
- Spin polarized system (ISPIN = 2), another set of bands is given below for the other spin.

# Step 4: Run Xcrysden

## Result



- Ta-da !
- Fermi surface from each bands are given in individual tabs